Space–Time Coding for Broadband Wireless Communications

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Space–Time Coding for Broadband Wireless Communications
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Space–Time Coding for Broadband Wireless Communications

GEORGIOS B. GIANNAKIS
ZHIQIANG LIU
XIAOLI MA
SHENGLI ZHOU
To my parents, Sofia and Vassili
G. B. G.

To Guangmei and Gwyneth
Z. L.

To Xiangqian and my parents
X. M.

To Juanjuan and Daniel
S. Z.
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