TRANSPORT PHENOMENA FOR CHEMICAL REACTOR DESIGN

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This book is dedicated to Alphonse and all the women in my life: Olivia, Carol, Lorraine, Jenny, Sarah, and Sally. Buddy and Pookie were also inspirational. It is an environmentally friendly book because all proceeds will be used to support motorless motion in Colorado’s clean air above 10,000 feet, particularly the ascent of Mount Evans at 14,260 feet from Bergen Park (i.e., the highest paved road on the planet), which, along with col de la Bonette at 2830 meters northwest of St. Etienne de Tinee and southeast of Barcelonnette (i.e., the highest paved road in Europe), is one of the most awesome bike rides on the planet.
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